



Exercise 1

1.1

$$\begin{aligned} &\text{Maximize } F(x_1, x_2) = x_1 + 2x_2 \\ &\text{subject to } 2x_1 + x_2 \leq 4 \\ &\quad x_1, x_2 \geq 0 \end{aligned}$$

1.2

$$\begin{aligned} &\text{Minimize } f(x_1, x_2) = x_1 + 3x_2 \\ &\text{subject to } x_1 + 4x_2 \geq 48 \\ &\quad 5x_1 + x_2 \geq 50 \\ &\quad x_1, x_2 \geq 0 \end{aligned}$$

1.3

$$\begin{aligned} &\text{Minimize } f(x_1, x_2) = 5x_1 + 10x_2 \\ &\text{subject to } 10x_1 + 5x_2 \leq 50 \\ &\quad 5x_1 - 5x_2 \geq -20 \\ &\quad x_1, x_2 \geq 0 \end{aligned}$$

1.4

$$\begin{aligned} &\text{Minimize } f(x_1, x_2) = 3x_1 + x_2 \\ &\text{subject to } 2x_1 + 4x_2 \leq 21 \\ &\quad 5x_1 + 3x_2 \leq 18 \\ &\quad x_1, x_2 \geq 0 \end{aligned}$$

1.5

$$\begin{aligned} &\text{Minimize } f(x_1, x_2) = 3x_1 + 6x_2 \\ &\text{subject to } -3x_1 + 3x_2 \leq 2 \\ &\quad 4x_1 + 2x_2 \leq 4 \\ &\quad -x_1 + 3x_2 \geq 1 \end{aligned}$$



1.6

$$\text{Maximize } f(x_1, x_2) = 50x_1 + 40x_2$$

$$\text{Subject to } 2x_1 + 4x_2 \leq 8$$

$$x_1 + 2x_2 \leq 4$$

$$x_1, x_2 \geq 0$$

1.7 A factory manufactures two machines A and B. The maximum number of machines that can be manufactured daily is 20. The shipping facility can handle no more than 14 machines per day. If the prices of machines A and B are L.E. 3000 and L.E. 5500, respectively. How many A and B machines should the company manufacture every day to maximize its profit?

1.8 A trucking company wants to purchase two new trucks. It has \$3 million to spend. The prices of the two kinds of trucks are \$30 thousands and \$50 thousands. There are some limitations on the operations that need to be considered. The company can hire at most 50 truck drivers. Garage and maintenance facilities can handle at the most 25 trucks. How many trucks of each type should the company purchase?